

# Optics Letters

## Tunable hybrid silicon nitride and thin-film lithium niobate electro-optic microresonator

ABU NAIM R. AHMED,<sup>1,\*</sup> SHOUYUAN SHI,<sup>1</sup> MATHEW ZABLOCKI,<sup>1</sup> PENG YAO,<sup>2</sup> AND DENNIS W. PRATHER<sup>1</sup>

<sup>1</sup>School of Electrical and Computer Engineering, University of Delaware, Newark, Delaware 19716, USA

<sup>2</sup>Phase Sensitive Innovations, Newark, Delaware 19711, USA

\*Corresponding author: naimece@udel.edu

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**This Letter presents, to the best of our knowledge, the first hybrid Si<sub>3</sub>N<sub>4</sub>-LiNbO<sub>3</sub>-based tunable microring resonator where the waveguide is formed by loading a Si<sub>3</sub>N<sub>4</sub> strip on an electro-optic (EO) material of X-cut thin-film LiNbO<sub>3</sub>. The developed hybrid Si<sub>3</sub>N<sub>4</sub>-LiNbO<sub>3</sub> microring exhibits a high intrinsic quality factor of 1.85 × 10<sup>5</sup>, with a ring propagation loss of 0.32 dB/cm, resulting in a spectral linewidth of 13 pm, and a resonance extinction ratio of ~27 dB within the optical C-band for the transverse electric mode. Using the EO effect of LiNbO<sub>3</sub>, a 1.78 pm/V resonance tunability near 1550 nm wavelength is demonstrated.** © 2019 Optical Society of America

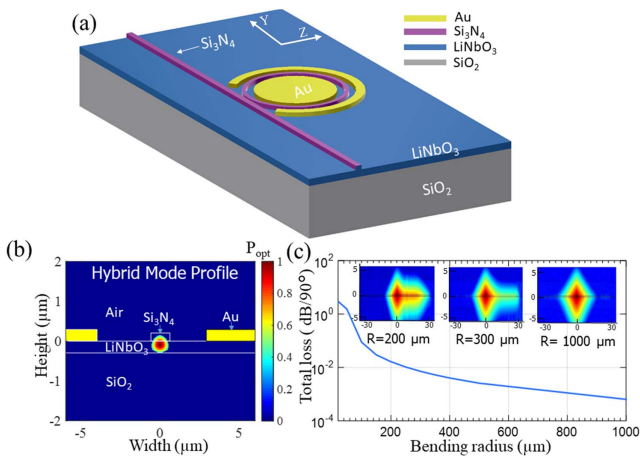
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Modern technology has stepped into the era of the Internet of Things (IoT), on-chip data centers, superconducting quantum computers, artificial intelligence (AI), 5G networks, etc., of which all these next-generation technologies demand low drive power, ultrawide bandwidth, high-speed data transmission, small footprint, and a complementary metal-oxide-semiconductor (CMOS)-compatible fabrication process. Capable of simultaneously addressing these challenges, optical interconnect has generated great interest in recent years [1–6]. Accordingly, the microring resonator is considered a key building block of an optical interconnect fabric, as it is essential for all-optical switching, high-speed modulation, tunable optical filters, optical frequency comb generation, laser resonators, compact footprint, etc. [7]. Historically, microring resonators have been widely investigated in different material systems including Si [7–9], Si<sub>3</sub>N<sub>4</sub> [9,10], graphene-Si [11], LiNbO<sub>3</sub> [12–16], Si-LiNbO<sub>3</sub> [17–20], Si-GaN [21], InP [22], AlN [23], GaAs [24], polymers [25], chalcogenide [26], etc. The tuning methods explored in these materials include the plasma dispersion effect, the thermo-optic effect, the electro-absorption effect, electro-optomechanics, and the electro-optic (EO) effect [12,17,26,27]. Unfortunately, many of them suffer from drawbacks and limitations including low modulation bandwidth, low extinction ratio, temperature sensitivity, nonlinearity, low modulation efficiency, aging, stability, scalability, and large footprint [12,14,23,26,27]. Recently the crystal-ion-sliced (CIS) thin-film LiNbO<sub>3</sub> on insulator

(LNOI) platform has excited a lot of attention due to its superior advantages, such as tight optical mode confinement, high EO modulation efficiency, linear voltage-index relationship, ultrawide operational bandwidth, low drive power, high extinction ratio, and small bending radii [16–19,28–30]. Both standalone and hybrid LiNbO<sub>3</sub> platforms (e.g., Si-LiNbO<sub>3</sub>, Si<sub>3</sub>N<sub>4</sub>-LiNbO<sub>3</sub>) [28–33] are very active in the related research fields. While most recent work has successfully demonstrated a low optical loss in standalone LiNbO<sub>3</sub> by the plasma-etching method [13,14] to form waveguide guiding, the hybrid platform still remains as an open research field owning its potential hybrid integration with the CMOS-compatible manufacturing process and driving circuitry. Moreover, LiNbO<sub>3</sub> is a material that presents difficulties when trying to etch, so the etch processes of LiNbO<sub>3</sub> are still underdeveloped compared to those in silicon-based materials. The hybrid platform circumvents this difficulty by utilizing a more conventional film and etch of silicon-based materials to enabling waveguiding in a LiNbO<sub>3</sub>, without the requirement of etching the LiNbO<sub>3</sub> itself. Previously, hybrid Si-LiNbO<sub>3</sub>-based microring resonators have been extensively reported in the literature [18–21]. Microring devices based on the Si<sub>3</sub>N<sub>4</sub>-LiNbO<sub>3</sub> material have yet to be studied. Si<sub>3</sub>N<sub>4</sub>-LiNbO<sub>3</sub> comes forward as a promising material system due to better index matching, high mode confinement inside LiNbO<sub>3</sub> [32–34], the ultralow propagation loss of Si<sub>3</sub>N<sub>4</sub>, high power handling capabilities, Si<sub>3</sub>N<sub>4</sub> insulating properties, and a wide optical transparency window [35]. Previous Si<sub>3</sub>N<sub>4</sub>-LiNbO<sub>3</sub>-based work focuses primarily on passive devices with vertical mode transition structures from Si<sub>3</sub>N<sub>4</sub> to LiNbO<sub>3</sub> material [32,33] and push-pull Mach-Zehnder interferometer (MZI) modulation [34]. Furthermore, most of the prior hybrid material systems were realized by bonding LNOI onto the strip-loaded waveguide structure [18,28,31–33], which is challenging due to reliability, fabrication, and design complexity (handle removal), and electrode fabrication process.

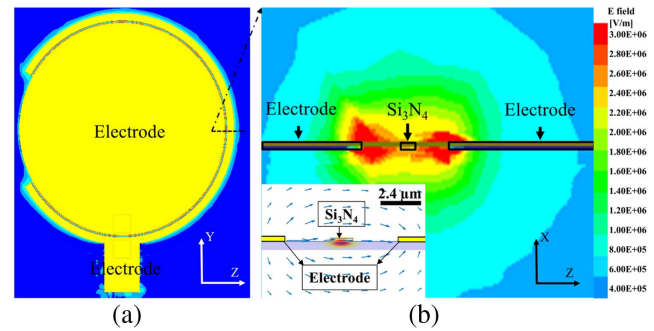
In this Letter, the first hybrid Si<sub>3</sub>N<sub>4</sub>-LiNbO<sub>3</sub>-based high-*Q* active microring resonator is presented, where plasma-enhanced chemical vapor deposition (PECVD) Si<sub>3</sub>N<sub>4</sub> thin film was directly deposited on an LNOI wafer to define the strip-loaded waveguide structure, eliminating the postfabrication



**Fig. 1.** (a) Schematic of the tunable hybrid Si<sub>3</sub>N<sub>4</sub>-LiNbO<sub>3</sub> microring resonator with integrated electrodes (not drawn in scale). (b) Simulated TE mode field profile of a hybrid Si<sub>3</sub>N<sub>4</sub>-LiNbO<sub>3</sub> waveguide formed by a 200 nm × 1.2 μm Si<sub>3</sub>N<sub>4</sub> loading strip at 1550 nm. (c) Simulated bending loss as a function of bending radius for the TE mode. The bending loss is presented as decibel (dB) per 90° bend.

processes, such as bonding and handle removal. The device consists of a microring and a coupled straight bus waveguide, exhibiting high intrinsic  $Q$ -factors of  $1.8 \times 10^5$  with a small resonant linewidth of 13 pm. The measured extinction ratio and ring loss are  $\sim 27$  dB and 0.32 dB/cm, respectively, near 1550 nm, within the optical C-band. Finally, the EO tuning of the microring is demonstrated, achieving a tunability of 1.78 pm/V.

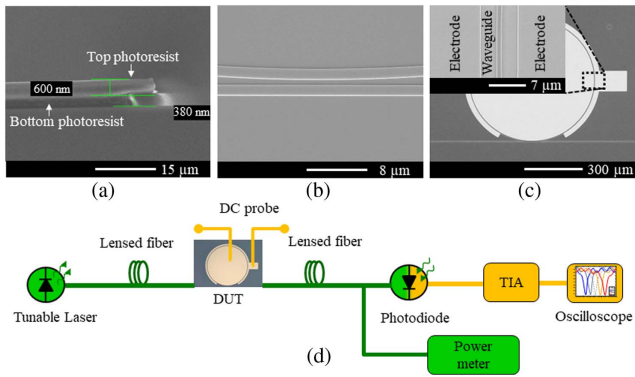
The schematic of the tunable Si<sub>3</sub>N<sub>4</sub>-LiNbO<sub>3</sub> hybrid microring structure is shown in Fig. 1(a). The cross section illustrated in Fig. 1(b) shows the optical waveguide consisting of a Si<sub>3</sub>N<sub>4</sub> strip placed on the top of the 300 nm  $X$ -cut thin-film LiNbO<sub>3</sub> and a 2 μm SiO<sub>2</sub> bottom cladding layer. The thickness and width of the Si<sub>3</sub>N<sub>4</sub> strip are 200 nm and 1.2 μm, respectively, chosen such that they support a single transverse electric (TE)-polarized fundamental mode at a wavelength of 1550 nm. The optimal device dimensions are chosen such that the optical mode is mostly confined in the LiNbO<sub>3</sub> and to ensure minimum bending loss. The complete mode confinement factor map in the LiNbO<sub>3</sub> ( $\Gamma_{LN}$ ) was studied in a previous work [33] using Lumerical software modules. The mode confinement factor in the LiNbO<sub>3</sub> is  $\sim 65\%$  for the above-mentioned structure. The bending loss for different bend radii is studied using Lumerical Mode Solver shown in Fig. 1(c). At a bending radius of 200 μm, the bending loss is below 0.1 dB/90° bend, though the logarithmic mode profile in the inset shows an asymmetric mode distribution. In this work, a 300 μm bending radius is chosen to ensure bending loss below 0.01 dB/90° bend, and the logarithmic mode profile is closer to the straight waveguide section. The refractive index of the PECVD Si<sub>3</sub>N<sub>4</sub> used within the model is 1.94, which is consistent with the experimental value. The final structure consists of a 300 μm ring radius, which is side coupled to a straight bus waveguide. EO tuning of the microring resonator is achieved by patterning signal and ground gold electrodes on the LNOI substrate on both the sides of the optical waveguide for the  $X$ -cut LiNbO<sub>3</sub> configuration. This configuration offers a strong mode



**Fig. 2.** (a) Simulated electric field distribution of the microring with 10 V voltage applied between the ground signal electrodes. (b) The electric field distribution in the cross section indicates the field concentration near 2 MV/m under the Si<sub>3</sub>N<sub>4</sub> strip waveguide. The inset shows the simulated RF electric field direction (arrows) of the device's cross section.

overlap between the fundamental TE-polarized light and the applied electric field with the LiNbO<sub>3</sub> crystal axis. The modulating electrodes are placed around the microring resonator except for the region immediately surrounding the optical coupling section from the bus so that an applied voltage does not impact the coupling between the ring and bus waveguide. The gap between the ground and signal electrodes and the thickness are 7 μm and 250 nm, respectively. The electrode gap is chosen such that it ensures low metal absorption loss and maximum optical and electric field overlap. The simulated electric field distributions for the top view and the cross-sectional view of the structure are shown in Fig. 2(a) and Fig. 2(b), respectively. The simulation is performed by ANSYS high frequency structure simulator (HFSS), and the electric field under the Si<sub>3</sub>N<sub>4</sub> waveguide is about 2 MV/m for a 10 V applied voltage. The strong electric field concentration in the LiNbO<sub>3</sub> EO material will induce a significant optical index change, and thus efficient EO modulation.

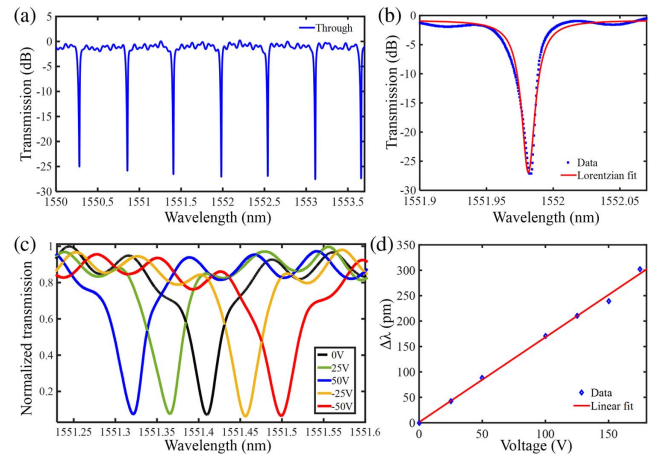
The thin-film CIS LNOI is procured from NanoLN. The 3" wafer consists of a 300 nm thick layer of an  $X$ -cut LiNbO<sub>3</sub> device layer bonded to a 500 μm thick quartz handle wafer via a 2 μm PECVD SiO<sub>2</sub> intermediate layer. The fabrication process of the microring consists of three main steps: PECVD Si<sub>3</sub>N<sub>4</sub> deposition, e-beam lithography (EBL) for microring definition, and electrode fabrication. To form the hybrid device, a thin film of a Si<sub>3</sub>N<sub>4</sub> layer is deposited on top of the thin-film LiNbO<sub>3</sub> using PECVD. Although PECVD Si<sub>3</sub>N<sub>4</sub> is lossy compared to the low-pressure chemical vapor deposition (LPCVD) due to the residual hydrogen content, the LPCVD high processing temperature produces cracks in LiNbO<sub>3</sub>. The optical loss can be further improved by introducing a glass cladding layer or reducing the hydrogen content in the Si<sub>3</sub>N<sub>4</sub> by sputtering or other low temperature deposition techniques [36]. A 200 nm of PECVD Si<sub>3</sub>N<sub>4</sub> is deposited using the following parameters: SiH<sub>4</sub>/NH<sub>3</sub>/N<sub>2</sub>, 10 sccm/6 sccm/300 sccm, a chamber pressure of 100 Pa, RF power of 50 W, and temperature of 300°C. The deposition rate is 42.85 nm/min, and the measured refractive index is 1.943 at 1550 nm. The microring and the waveguide are defined on the Si<sub>3</sub>N<sub>4</sub> layer by EBL using a similar process as described in a previous work [33]. The metal electrodes are defined on top of the LiNbO<sub>3</sub> layer as a ground signal configuration. A bilayer lift-off process and



**Fig. 3.** (a) SEM image of the bilayer lift-off process. (b) SEM image of the microring coupling section. (c) SEM image of a hybrid  $\text{Si}_3\text{N}_4$ - $\text{LiNbO}_3$  microring with a bending radius of  $300\ \mu\text{m}$ , waveguide thickness of  $200\ \text{nm}$ , and waveguide width of  $1.2\ \mu\text{m}$ . The inset shows the zoomed section of the boxed region. (d) Schematic of the experimental setup for measuring the transmission spectrum and electro-optically tuning the resonant wavelength in the hybrid microring.

evaporation process are performed to pattern the metal electrode. We use LOR-5A (MicroChem Corp) and AZ MIR 701 (MicroChemicals) photoresists in a positive-tone mode in this bilayer process. The LOR-5A is coated first, followed by the AZ MIR 701 coating. The electrodes are patterned using the laser writer (Heidelberg MLA 100), which maintains high-precision alignment with the microring structure. After lithography, both the resists are developed at the same time using AZ 300 MIF developer. The bilayer lift-off process creates an undercut profile [Fig. 3(a)], which helps to define fine pattern and achieve clean solvent lift-off. A brief plasma descum is performed before metal evaporation to remove photoresist residue and establish good metal adhesion. Next, a  $20\ \text{nm}$  Ti layer followed by a  $250\ \text{nm}$  Au layer are deposited via e-beam evaporation. Then the metal lift-off is performed in the NMP solvent (1-methyl-2-pyrrolidinone) at  $80^\circ\text{C}$  in the ultrasonic bath. Finally, the device's waveguide facets are diced and polished for fiber-chip coupling. The scanning electron micrograph (SEM) image of the fabricated microring coupling section and the microring with the integrated electrode are shown in Figs. 3(b) and 3(c).

The fabricated hybrid microring resonator is characterized by extracting the transmission spectrum using a Keysight tunable laser swept at wavelengths surrounding  $1550\ \text{nm}$ . The experimental setup is shown in Fig. 3(d). The tunable laser source is coupled to the device under test (DUT) using a lensed fiber, which is aligned to launch TE-polarized light. The output light is detected and monitored on an oscilloscope with the assistance of a transimpedance amplifier (TIA). The measured transmission spectrum of the single bus microring resonator around  $1550\ \text{nm}$  is shown in Fig. 4(a). The periodic dips and uniform spacing between adjacent dips indicate that only one mode is present inside the microring. The measured free spectral range (FSR) and the spectral linewidth of the microring are  $\Delta\lambda_{\text{FSR}} = 0.58 \pm 0.004\ \text{nm}$  and  $\delta\lambda_{\text{FWHM}} = 0.013 \pm 0.0006\ \text{nm}$ . The maximum potential extinction ratio is about  $26.92\ \text{dB}$  at  $1551.98\ \text{nm}$ . The intrinsic quality factor of  $1.85 \times 10^5$  at  $1551.98\ \text{nm}$  is extracted by fitting the central transmission



**Fig. 4.** Hybrid microring resonator characterization. (a) The measured transmission spectrum of the passive microring at the through port for TE mode using a tunable laser near  $1550\ \text{nm}$ . The free spectral range is  $0.58\ \text{nm}$ , and the resonance extinction ratios are up to  $27\ \text{dB}$ . (b) The Lorentz fitting (red curve) of the resonance dip at  $1551.98\ \text{nm}$ , which corresponds to an intrinsic  $Q$  of  $1.83 \times 10^5$ . (c) The resonant spectra as a function of the applied voltage for TE mode at wavelengths near  $1551.410\ \text{nm}$  (black curve); the red and blue curves are the corresponding electro-optically shifted curves by applying a voltage of  $-50\ \text{V}$  and  $+50\ \text{V}$  to the device electrodes, respectively. The measured tunability is  $1.78\ \text{pm/V}$ . (d) The resonant wavelength shift as a function of the applied DC voltage.

dip with a Lorentzian [37] as shown in Fig. 4(b). The loss per unit length in the ring [37] is calculated as  $0.32\ \text{dB/cm}$ . The microring resonator tuning ability is characterized by the transmission spectrum shift by applying different voltages to the device electrodes. The applied voltage will change the refractive index of the  $\text{LiNbO}_3$  due to its EO properties, which causes a phase change and shifts the resonance condition. The experimental setup is the same as Fig. 3(d). The DC bias is applied to the top of the integrated electrodes using a voltage source and DC probe to a ring resonator centered at  $1551.410\ \text{nm}$ . The bias voltage is varied from  $+50\ \text{V}$  to  $-50\ \text{V}$  to demonstrate wavelength tuning spectra shown in Fig. 4(c). The measured results indicate a total of  $178.4\ \text{pm}$  wavelength shift when the voltage changes from  $+50\ \text{V}$  to  $-50\ \text{V}$ . Figure 4(d) shows the wavelength shift as a function of the applied voltage, which shows a linear dependence of the wavelength shift on the applied voltage. The measured tuning coefficient is  $1.784\ \text{pm/V}$ . As a result, only  $\sim 7\ \text{V}$  driving voltage is required to tune over a spectral range of a spectral width of  $13\ \text{pm}$ . The tunability can be further improved by reconfiguring the electrode design and microring structure [38,39].

In summary, the presented work demonstrates a high- $Q$  and tunable hybrid microring resonator where a potential photonic platform for future photonic integrated circuit (PIC) based on  $\text{Si}_3\text{N}_4$  on thin-film  $\text{LiNbO}_3$  has been explored. This is the first time, to the best of our knowledge, that a hybrid  $\text{Si}_3\text{N}_4$ - $\text{LiNbO}_3$ -based tunable microring resonator with high- $Q$  has been fabricated and characterized. The fabrication process involved simple PECVD  $\text{Si}_3\text{N}_4$  deposition on the LNOI and waveguide pattern on  $\text{Si}_3\text{N}_4$ , simplifying electrode

design and fabrication methods. The fabricated microring resonator demonstrated a high intrinsic  $Q$  of  $1.85 \times 10^5$  and resonance extinction ratio of  $\sim 27$  dB at optical C-band for the TE mode. For the TE mode, microelectrodes are patterned on top of the  $\text{LiNbO}_3$  surface to tune the microring electro-optically. A  $1.78$  pm/V tunability of the resonant wavelength and a linear wavelength change ( $\Delta\lambda$ ) voltage relationship were observed. The current work will encourage future research on the development of the  $\text{Si}_3\text{N}_4$ - $\text{LiNbO}_3$  platform for the development of complex, high-performance future PIC.

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